## "The Trans-Carpathian Seminar on Geometry & Physics"

(See also the Geometry & Physics @ DFT seminar homepage)

Date: Wednesday, Dec 17, 2025, 15:15 EET (Bucharest time)

Location: online via Zoom

Speaker: Rafal Suszek (KMMF, University of Warsaw)

## Title: Stacky Dynamics in the Shadows of Principaloid Bundles

Abstract: A novel definition shall be presented of a gauge(d) field theory with the configuration bundle given by the Godement quotient F (aka the shadow) of a principaloid bundle with connection  $(P,\Theta)$ , introduced by Strobl and the speaker earlier this year, with respect to the defining action of its structure Lie groupoid  $G \Longrightarrow M$ . The field theory shall be descended from a two-dimensional Polyakov-Alvarez-Gawedzki  $\sigma$ -model with target M, the latter being endowed with a metric  $g_M$  and a bundle gerbe  $\mathcal G$  with connective structure of curvature  $H \in Z^3(M)$ , which codetermines the  $\sigma$ -model through the corresponding degree-3 Cheeger-Simons differential character (aka the surface holonomy). It is to be viewed as an effective formulation of charged-loop dynamics on the characteristic foliation M // G, consistent with the principle of homogeneity of internal structures (configurational degrees of freedom, gauges etc.) over the spacetime of the field theory.

The crucial role of a prequantisable multiplicative Bott-Shulman-Stasheff extension  $(H, \rho)$  of the gerbe's curvature H (turning  $G \Longrightarrow M$  into a Laurent-Gengoux-Xu prequantisable pre-quasi-symplectic groupoid), and that of a combined  $g_M$ -isometric and  $\rho$ -holonomic reduction of the structure group  $Bisec(G \Longrightarrow M)$  of P shall be emphasised in a coherent descent of the  $\sigma$ -model to F from its local trivialisation. The latter employs the structure of a smooth 2-stack on bundle gerbes with connective structure (which shall be explained), alongside an augmentation of G that hinges on a canonical coupling between the comomentum component of the Spencer operator of  $\rho$ , as defined by Crainic et al., and the connection  $\Theta$ . Time permitting, the abstract mechanism shall be illustrated with the example of the physically and mathematically important and much-studied Alekseev-Malkin-Meinrenken quasi-symplectic groupoid.

The talk is planned for 2x45 min.