



TACHYONS AND REHEATING IN A BRANEWORLD INFLATIONARY SCENARIO

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N. Bilic, S. Domazet, . G. Djordjevic ***Tachyon with an inverse power-law potential in a braneworld cosmology***,

Class. Quantum Grav. 34 (2017) 165006, **arXiv:1704.01072**

Bilic, S. Domazet, . G. Djordjevic, ***Particle creation and reheating in a braneworld inflationary scenario***

Phys. Rev. D 96, 083518 (2017), arXiv:1707.06023

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OUTLINE

- Introduction and motivation
- Tachyon Inflation
- Braneworld universe and Randall - Sundrum Models (RSI/RSII)
- Numerical results
- Tachyon with an inverse power-law potential
- Ongoing Research and Conclusion

INTRODUCTION AND MOTIVATION

Background of personal motivation

Conjectures and papers of Ashoka Sen and others

a) tachyon matter

b) nonarchimedean/ p -adic mathematical background of strings, branes and tachyons

- p -Adic numbers and nonarchimedean geometry in physics (Volovich, Dragovic ...)
- p -Adic and adelic strings (Volovich, Freund, Witten, Shatashvili, Zwiebach ...)
- p -Adic inflation (Barnaby, Cline, Koshelev ...)

INTRODUCTION AND MOTIVATION

- The inflationary universe scenario in which the early universe undergoes a rapid expansion has been generally accepted as a solution to the horizon problem and some other related problems of the standard big-bang cosmology
- Quantum cosmology: probably the best way to describe the evolution of the early universe, however ...
- Recent years - a lot of evidence from WMAP and Planck observations of the CMB

OBSERVATIONAL PARAMETERS

- Hubble hierarchy (slow-roll) parameters

$$\dot{\epsilon}_{i+1} \equiv \frac{d \ln |\dot{\epsilon}_i|}{dN}, \quad i \geq 0, \quad \dot{\epsilon}_0 \equiv \frac{H_*}{H}$$

Hubble rate at an arbitrarily chosen time

- Length of inflation $e_i = 1$

- $$N(\phi) = \ln \frac{a_{end}}{a} = \int_t^{t_{end}} d \ln a = \int_t^{t_{end}} H dt = \int_{\phi}^{\phi_{end}} \frac{H}{\dot{\phi}} d\phi \approx \frac{1}{M_{\text{Pl}}^2} \int_{\phi_{end}}^{\phi} \frac{V}{V'} d\phi$$

- The end of inflation $\dot{\epsilon}_i(\phi_{end}) \approx 1$
- Three independent observational parameters: amplitude of scalar perturbation A_s , tensor-to-scalar ratio r and scalar spectral index n_s

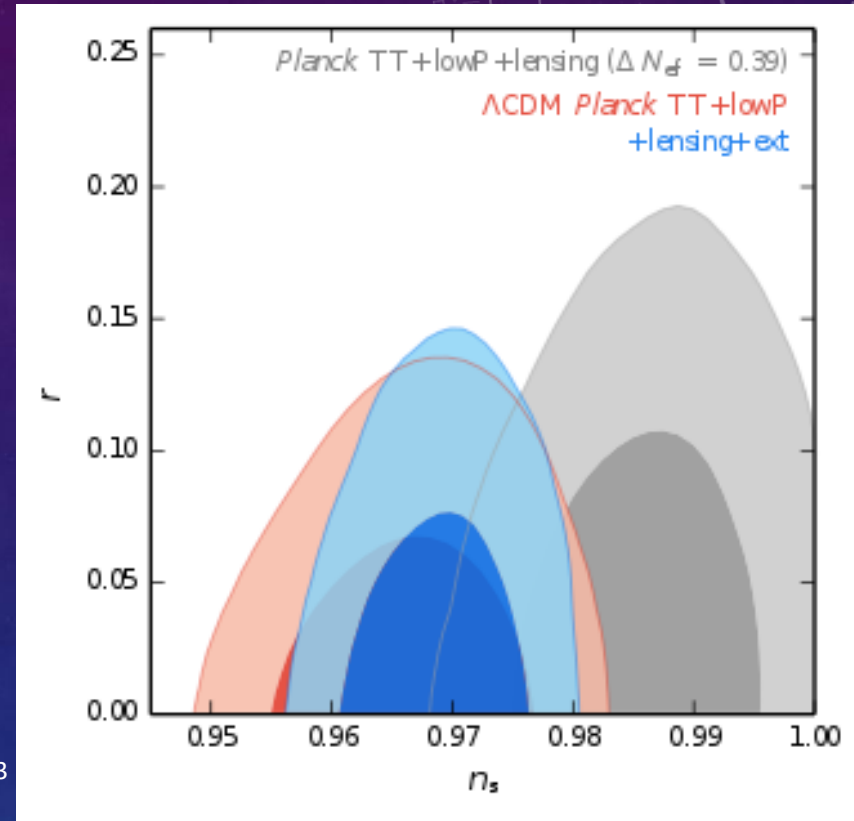
$$r = 16\epsilon_1$$

$$n_s = 1 - 2\epsilon_1 - \epsilon_2$$

At the lowest order in parameters ϵ_1 and ϵ_2

OBSERVATIONAL PARAMETERS

- Satellite Planck
(May 2009 – October 2013)
- Latest results are published
in year 2016.



Planck 2015 results: XIII. Cosmological parameters, *Astronomy & Astrophysics*. 594 (2016) A13
 Planck 2015 results. XX. Constraints on inflation, *Astronomy & Astrophysics*. 594 (2016) A20

Model	Parameter	Planck TT+lowP	Planck TT+lowP+lensing	Planck TT+lowP+BAO	Planck TT,TE,EE+lowP
$\Lambda\text{CDM}+r$	n_s	0.9666 ± 0.0062	0.9688 ± 0.0061	0.9680 ± 0.0045	0.9652 ± 0.0047
	$r_{0.002}$	< 0.103	< 0.114	< 0.113	< 0.099
$\Lambda\text{CDM}+r$ + $dn_s/d \ln k$	n_s	0.9667 ± 0.0066	0.9690 ± 0.0063	0.9673 ± 0.0043	0.9644 ± 0.0049
	$r_{0.002}$	< 0.180	< 0.186	< 0.176	< 0.152
	r	< 0.168	< 0.176	< 0.166	< 0.149
	$dn_s/d \ln k$	$-0.0126^{+0.0098}_{-0.0087}$	$-0.0076^{+0.0092}_{-0.0080}$	-0.0125 ± 0.0091	-0.0085 ± 0.0076

LAGRANGIAN OF A SCALAR FIELD - $\mathcal{L}(X, \phi)$

- In general case – any function of a scalar field ϕ and kinetic energy $X \equiv \frac{1}{2} \partial_\mu \phi \partial_\nu \phi$.

- Canonical field, potential $V(\phi)$

$$\mathcal{L}(X, \phi) = BX - V(\phi),$$

- Non-canonical models

$$\mathcal{L}(X, \phi) = BX^n - V(\phi),$$

- Dirac-Born-Infeld (DBI) Lagrangian

$$\mathcal{L}(X, \phi) = -\frac{1}{f(\phi)} \sqrt{1 - 2f(\phi)X} - V(\phi),$$

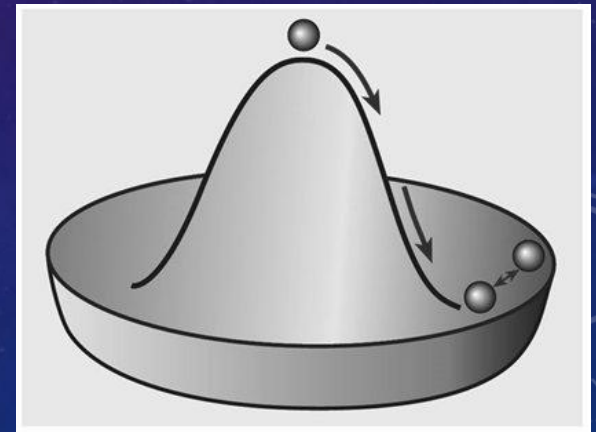
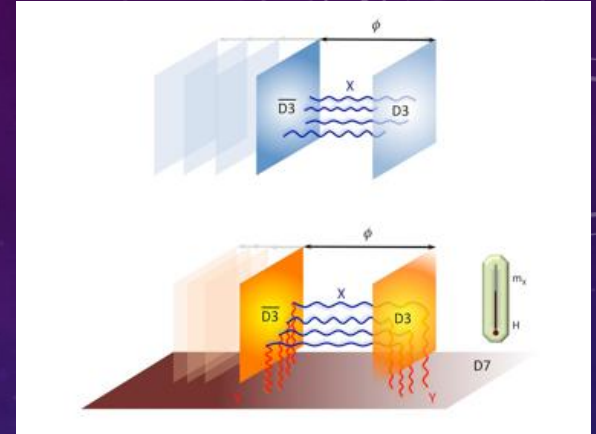
- Special case – tachyonic $\mathcal{L}(X, \phi) = -V(\phi) \sqrt{1 - 2\lambda X}$,

TACHYONS

- Traditionally, the word tachyon was used to describe a hypothetical particle which propagates faster than light (Sommerfeld 1904 ?).
- In modern physics this meaning has been changed
 - The effective tachyonic field theory was **proposed** by A. Sen
 - **String theory**: states of quantum fields with imaginary mass (i.e. negative mass squared)
 - It **was believed**: such fields permitted propagation faster than light
 - However it **was realized** that the imaginary mass creates an instability and tachyons spontaneously decay through the process known as tachyon condensation

TACHYION FIELDS

- No classical interpretation of the "imaginary mass"
 - The instability: The potential of the tachyonic field is initially at a local maximum rather than a local minimum (like a ball at the top of a hill)
 - A small perturbation - forces the field to roll down towards the local minimum.
 - Quanta are not tachyon any more, but rather an "ordinary" particle with a positive mass.



REFERENCES: TACHYONS' QUANTIZATION – (NON)ARCHIMEDEAN SPACES

- D.D. Dimitrijevic, G.S. Djordjevic and Lj. Netic,
Real and p-Adic aspects of quantization of tachyons,
in Mathematical, theoretical and phenomenological
challenges beyond the standard model, World
scientific (2005) 197-207, (eds) G. S. Djordjevic, Lj.
Netic and J. Wess
- D.D. Dimitrijevic, G.S. Djordjevic and Lj. Netic
Fortschritte der Physik, **56** No. 4-5 (2008) 412-417
- Dragoljub D. Dimitrijevic, G. S. Dj and Milan Milosevic
Classicalization and Quantization of Tachyon-like
Matter on (non)Archimedean Spaces, Rom.Rep.Phys.
68 (2016) No 1, 5

TACHYON INFLATION

- Consider the tachyonic field T minimally coupled to Einstein's gravity with action

$$S = -\frac{1}{16\pi G} \int \sqrt{-g} R d^4x + \int \sqrt{-g} \mathcal{L}(T, \partial_\mu T) d^4x$$

- Where R is Ricci scalar, and Lagrangian and Hamiltonian for tachyon potential $V(T)$ are

- $$\mathcal{L} = -V(T) \sqrt{1 - g^{\mu\nu} \partial_\mu T \partial_\nu T},$$

$$\mathcal{H} = \frac{V(T)}{\sqrt{1 - g^{\mu\nu} \partial_\mu T \partial_\nu T}}.$$

- Homogenous and isotropic space, FRW metrics

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu = dt^2 - a^2(t) d\vec{x}^2, \quad c = 1$$

TACHYON INFLATION

- As well as for a standard scalar field $P = \mathcal{L}$ i $\rho = \mathcal{H}$,
however:

$$\mathcal{L} = -V(T)\sqrt{1 - \dot{T}^2},$$

$$\mathcal{H} = \frac{V(T)}{\sqrt{1 - \dot{T}^2}}.$$

- Friedmann equation:

$$H^2 \equiv \left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{3M_P^2} \frac{V}{(1 - \dot{T}^2)^{1/2}}.$$

- Energy momentum conservation equation, $\dot{\rho} = -3H(P + \rho)$,
takes a form

$$\frac{\ddot{T}}{1 - \dot{T}^2} + 3H\dot{T} + \frac{V'}{V} = 0.$$

Reduced Planck mass

$$M_P = \sqrt{\frac{1}{8\pi G}}$$

TACHYON INFLATION

$$x = \frac{T}{T_0}, \quad \tau = \frac{t}{T_0}, \quad U(x) = \frac{V(x)}{\sigma}, \quad \tilde{H} = \frac{H}{T_0}.$$

- Non-dimensional equations

Energy-momentum conservation eq.

$$\ddot{x} + \kappa \sqrt{3U(x)(1 - \dot{x}^2)^{3/2}} \dot{x} + \frac{(1 - \dot{x}^2)}{U(x)} \frac{dU(x)}{dx} = 0$$

$$\tilde{H}^2 = \frac{\kappa^2}{3} \frac{U(x)}{\sqrt{1 - \dot{x}^2}}$$

Friedmann eq.

$$\dot{\tilde{H}} = -\frac{\kappa^2}{2} (\tilde{P} + \tilde{\rho})$$

Friedmann acceleration eq.

- Dimensionless constant $\kappa^2 = \frac{\sigma T_0^2}{M_{Pl}^2}$, a choice of a constant σ (brane tension) was motivated by string theory

$$\sigma = \frac{M_s^4}{g_s (2\pi)^3}.$$

CONDITION FOR TACHYON INFLATION

- General condition for inflation

$$\frac{\ddot{a}}{a} \equiv \tilde{H}^2 + \dot{\tilde{H}} = \frac{\kappa^2}{3} \frac{U(x)}{\sqrt{1 - \dot{x}^2}} \left(1 - \frac{3}{2} \dot{x}^2 \right) > 0.$$

- Slow-roll conditions

$$\ddot{x} \ll 3\tilde{H}\dot{x}, \quad \dot{x}^2 \ll 1.$$

- Equations for slow-roll inflation

$$\tilde{H}^2 \simeq \frac{\kappa^2}{3} U(x),$$
$$\dot{x} \simeq -\frac{1}{3\tilde{H}} \frac{U'(x)}{U(x)}.$$

INITIAL CONDITION FOR TACHYON INFLATION

- Basic ideas, problems (Steer, Vernizzi 2004)
- Slow-roll parameters

$$\epsilon_1 \simeq \frac{1}{2\kappa^2} \frac{U'^2}{U^3}, \quad \epsilon_2 \simeq \frac{1}{\kappa^2} \left(-2 \frac{U''}{U^2} + 3 \frac{U'^2}{U^3} \right).$$

- Number of e-folds

$$N(x) = \kappa \int_{x_i}^{x_e} \frac{U(x)^2}{|U'(x)|} dx$$

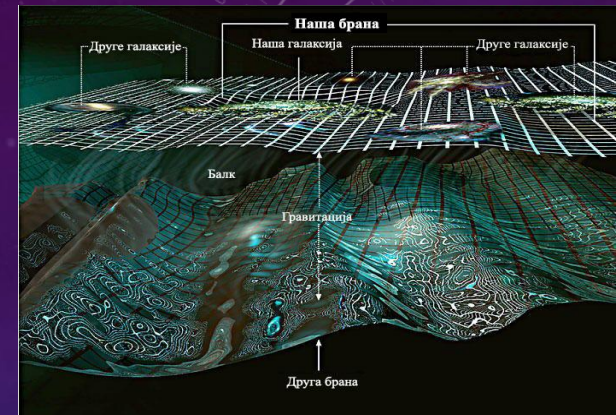
$$x_i = x(\tau_i)$$
$$x_e = x(\tau_e)$$

BRANEWORLD UNIVERSE

- Braneworld universe is based on the scenario in which matter is confined on a brane moving in the higher dimensional bulk with only gravity allowed to propagate in the bulk.
- N. Arkani-Hamed, S. Dimopoulos, and G. Dvali, Phys. Lett. B **429** (1998)
- L. Randall and R. Sundrum, Phys. Rev. Lett. **83** (1999) 3370 (RS I)
- L. Randall and R. Sundrum, Phys. Rev. Lett. **83** (1999) 4690 (RS II)
- 1998 ADD / 2000 DGP

D-BRANES, COSMOLOGY WITH EXTRA DIMENSIONS

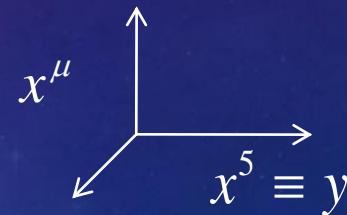
- 1999 – RSI and RSII
- We will consider the Randall-Sundrum scenario with a braneworld embedded in a 5-dim asymptotically Anti de Sitter space (AdS5)
- One of the simplest models
- Two branes with opposite tensions are placed at some distance in 5 dimensional space
- RSI model – observer reside on the brane with negative tension, distance to the 2nd brane corresponds to the Newtonian gravitational constant
- RSII – observer is placed on the positive tension brane, 2nd brane is pushed to infinity



RSI MODEL



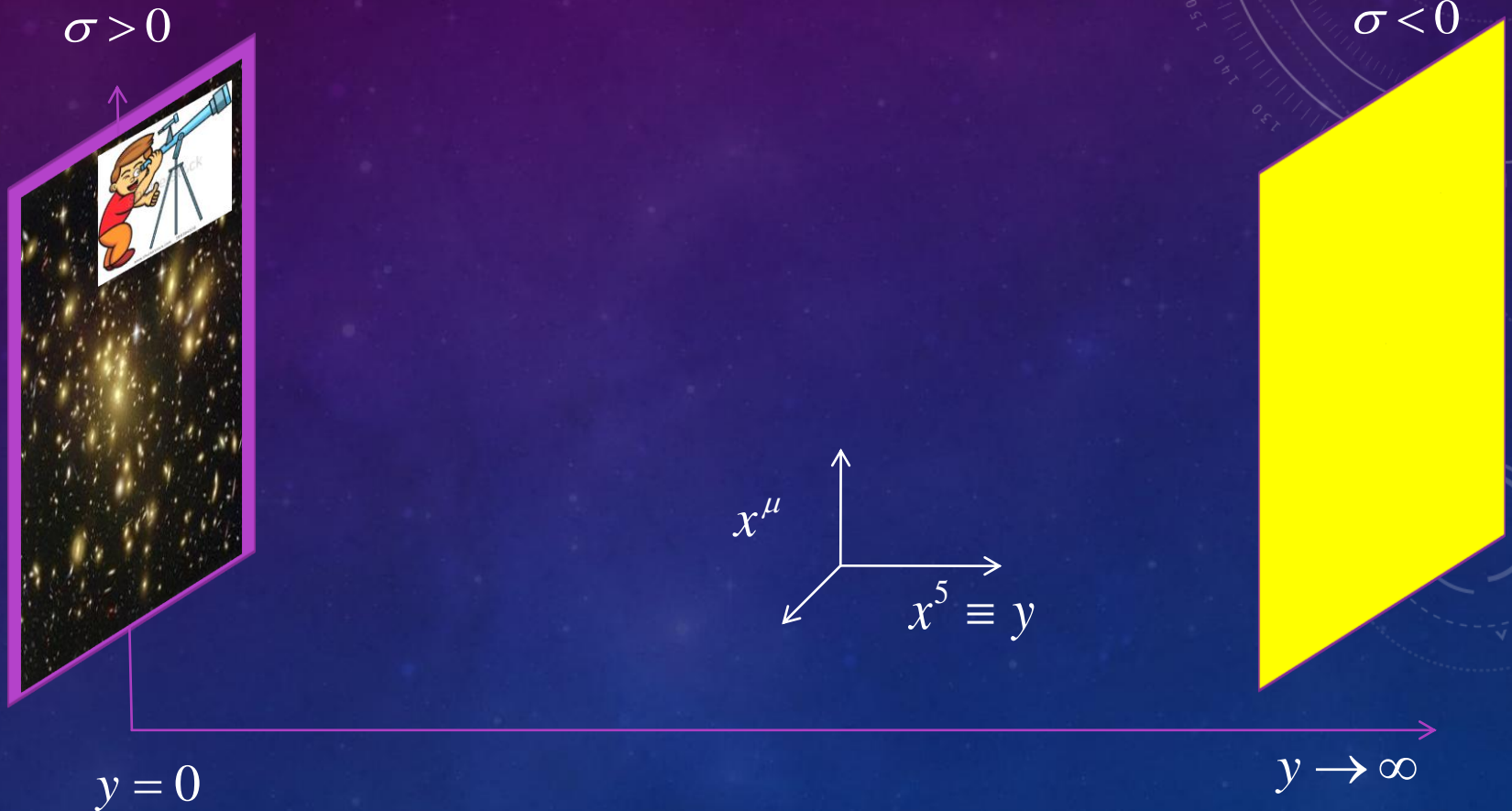
- Observers reside on the negative tension brane at $y = l$.
- The coordinate position $y = l$ of the negative tension brane serves as a compactification radius so that the effective compactification scale is $\mu_c = 1/l$.



$y \rightarrow \infty$

RSII MODEL

- Observers reside on the positive tension brane at
- $y = 0$ and the negative tension brane is pushed off to infinity in the fifth dimension.



RSII MODEL

- The space is described by Anti de Sitter metric

$$ds_{(5)}^2 = e^{-2ky} g^{\mu\nu} dx^\mu dx^\nu - dy^2.$$

- Extended RSII model includes radion backreaction

$$ds_{(5)}^2 = G_{ab} dX^a dX^b = \frac{1}{k^2 z^2} (1 + k^2 z^2 h(x)) g^{mn} dx^m dx^n - \frac{1}{(1 + k^2 z^2 h(x))^2} dz^2$$

$k = \frac{1}{l}$ ← AdS curvature radius
 ← Radion field

- Total action

$$S = S_{bulk} + S_{br} + S_{mat}.$$

- After integrating out 5th dimension...

RSII MODEL

- Action for a 3-brane moving in bulk

$$S = \int d^4x \sqrt{-g} \left[-\frac{R}{16pG} + \frac{1}{2} g^{mn} F_{,m} F_{,n} \right] + S_{\text{br}},$$

- Action for the brane

$$S_{\text{br}} = -s \int d^4x \sqrt{-\det g_{mn}^{\text{ind}}}$$

Brane tension

Canonical normalized radion field

$$h = \sinh^2 \left(\sqrt{\frac{4pG}{3}} \Phi \right)$$

$$= - \int d^4x \sqrt{-g} \frac{s}{k^4 Q^4} (1 + k^2 Q^2 h)^2 \sqrt{1 - \frac{g^{mn} Q_{,m} Q_{,n}}{(1 + k^2 Q^2 h)^3}}$$

- Without radion $\Phi = 0$

Tachyon field

$$Q = e^{ky} / k$$

$$S_{\text{br}}^{(0)} = - \int d^4x \sqrt{-g} \frac{l}{Q^4} \sqrt{1 - g^{mn} Q_{,m} Q_{,n}}, \quad l = \frac{s}{k^4}$$

- Total Lagrangian

$$L = \frac{1}{2} g^{mn} F_{,m} F_{,n} - \frac{l y^2}{Q^4} \sqrt{1 - \frac{g^{mn} Q_{,m} Q_{,n}}{y^3}}, \quad y = 1 + k^2 Q^2 h.$$

RSII MODEL

- In flat space, FRW metrics

$$ds^2 = g_{\mu\nu}dx^\mu dx^\nu = dt^2 - a^2(t)(dr^2 + r^2 d\Omega^2).$$

- Hamiltonian equations

$$\Pi_\Phi^\mu \equiv \frac{\partial L}{\partial \Phi_{,\mu}}, \quad \Pi_\Theta^\mu \equiv \frac{\partial L}{\partial \Theta_{,\mu}}.$$

- The Hamiltonian

$$\mathcal{H} = \frac{1}{2} \Pi_\Phi^2 + \frac{\lambda \psi^2}{\Theta^4} \sqrt{1 + \Pi_\Theta^2 \Theta^8 / (\lambda^2 \psi)}$$

RSII MODEL

- The Hamiltonian equations

$$\dot{\phi} = \frac{\partial H}{\partial P_F}$$

$$\dot{Q} = \frac{\partial H}{\partial P_Q}$$

$$\dot{P}_F + 3HP_F = - \frac{\partial H}{\partial F}$$

$$\dot{P}_Q + 3HP_Q = - \frac{\partial H}{\partial Q}$$

- The modified Friedman equation

$$H \circ \frac{\dot{a}}{a} = \sqrt{\frac{8pG}{3} H^2 + \frac{2pG}{3k^2} H^2}$$

- Combining with a continuity equation $\dot{\mathcal{H}} + 3H(\mathcal{H} + \mathcal{L}) = 0$ it leads to the second Friedman equation

$$\dot{H} = -4pG(H + L) + \frac{4pG}{3k^2} H^2$$

NONDIMENSIONAL EQUATIONS

$$h = H / k,$$

- Substitutions: $f = F / (k\sqrt{l}), p_f = P_F / (k^2\sqrt{l}),$
 $q = kQ, p_q = P_Q / (k^4l)$

$$\dot{\phi} = \pi_{\phi}$$

$$\dot{\theta} = \frac{\theta^4 \psi \pi_{\theta}}{\sqrt{1 + \theta^8 \pi_{\theta}^2 / \psi}}$$

$$\dot{\pi}_{\phi} = -3h\pi_{\phi} - \frac{\psi}{2\theta^2} \frac{4 + 3\theta^8 \pi_{\theta}^2 / \psi}{\sqrt{1 + \theta^8 \pi_{\theta}^2 / \psi}} \eta'$$

$$\dot{\pi}_{\theta} = -3h\pi_{\theta} + \frac{\psi}{\theta^5} \frac{4 - 3\theta^{10} \eta \pi_{\theta}^2 / \psi}{\sqrt{1 + \theta^8 \pi_{\theta}^2 / \psi}}$$

$$\left. \begin{aligned} \dot{h} &= -\frac{\kappa^2}{2} (\bar{\rho} + \bar{p}) \left(1 + \frac{\kappa^2}{6} \bar{\rho} \right) \\ \dot{N} &= h \end{aligned} \right\} \text{Additional equations, solved in parallel}$$

Nondimensional constant

$$\rightarrow \kappa^2 = 8\pi\lambda G k^2$$

Hubble parameter

$$\rightarrow h \equiv \frac{\dot{a}}{a} = \sqrt{\frac{\kappa^2}{3} \bar{\rho} \left(1 + \frac{\kappa^2}{12} \bar{\rho} \right)}$$

$$\psi = 1 + \theta^2 \eta,$$

$$\eta = \sinh^2 \left(\sqrt{\frac{\kappa^2}{6}} \phi \right),$$

$$\eta' = \frac{d\eta}{d\phi} = \sqrt{\frac{\kappa^2}{6}} \sinh \left(\sqrt{\frac{2\kappa^2}{3}} \phi \right),$$

Preasure

$$\rightarrow \bar{p} = \frac{1}{2} \dot{\phi}^2 - \frac{\psi^2}{\theta^4} \sqrt{1 - \dot{\theta}^2 / \psi^3},$$

Energy density

$$\rightarrow \bar{\rho} = \frac{1}{2} \dot{\phi}^2 + \frac{\psi^2}{\theta^4} \frac{1}{\sqrt{1 - \dot{\theta}^2 / \psi^3}}$$

INITIAL CONDITIONS FOR RSII MODEL

- Initial conditions – from a model without radion field
- “Pure” tachyon potential $V(\vartheta) = \frac{\lambda}{\vartheta^4}$
- Hamiltonian $\mathcal{H} = \frac{\lambda}{\vartheta^4} \sqrt{1 + \Pi_{\vartheta}^2 \vartheta^8 / \lambda^2}$.
- Nondimensional equation

$$\dot{q} = \frac{q^4 p_q}{\sqrt{1 + q^8 p_q^2}}$$
$$\dot{p}_q = -3h p_q + \frac{4}{q^5 \sqrt{1 + q^8 p_q^2}}.$$

ESTIMATION OF INITIAL CONDITIONS

- The end of inflation $\varepsilon_1 \approx 1$, t.j. $\kappa^2/\theta_f^4 \ll 1 \rightarrow$ RSII modification can be neglected

$$\dot{\phi}_1(q_f) ; \dot{\phi}_2(q_f) ; \frac{8q_f^2}{k^2} ; 1, \quad h(q_f) ; \frac{8}{\sqrt{3}k}.$$

- Number of e-folds

$$N ; \frac{k^2}{8q_0^2} \frac{\ddot{\phi}}{\dot{\phi}^2} + \frac{k^2}{36q_0^4} \frac{\ddot{\phi}}{\dot{\phi}^3}$$

- Number of e-folds (standard tachyon inflation)

$$N_{\text{st.tach}} ; \frac{k^2}{8q_0^2} - 1.$$

- Huge difference in number of e-folds \rightarrow RSII extends the period of inflation!!!

$$k^2 = 5, q_0 = 0,25 \quad \text{P} \quad \begin{cases} N_{\text{st.tach}} ; 9 \\ N ; 330 \end{cases}$$

OBSERVATIONAL PARAMETERS

- Scalar spectral index n_s and tensor-to-scalar ratio r (the first order of parameters ε_i)

$$r = 16\varepsilon_1(t_i),$$

$$n_s = 1 - 2\varepsilon_1(t_i) - \varepsilon_2(t_i)$$

- The second order of parameters $\varepsilon_i \rightarrow$ different

- $$r = 16e_1(1 + Ce_2 - 2ae_1),$$

$$n_s = 1 - 2e_1 - e_2 - \frac{2}{\epsilon}e_1^2 + (2C + 3 - 2a)e_1e_2 + Ce_2e_3$$

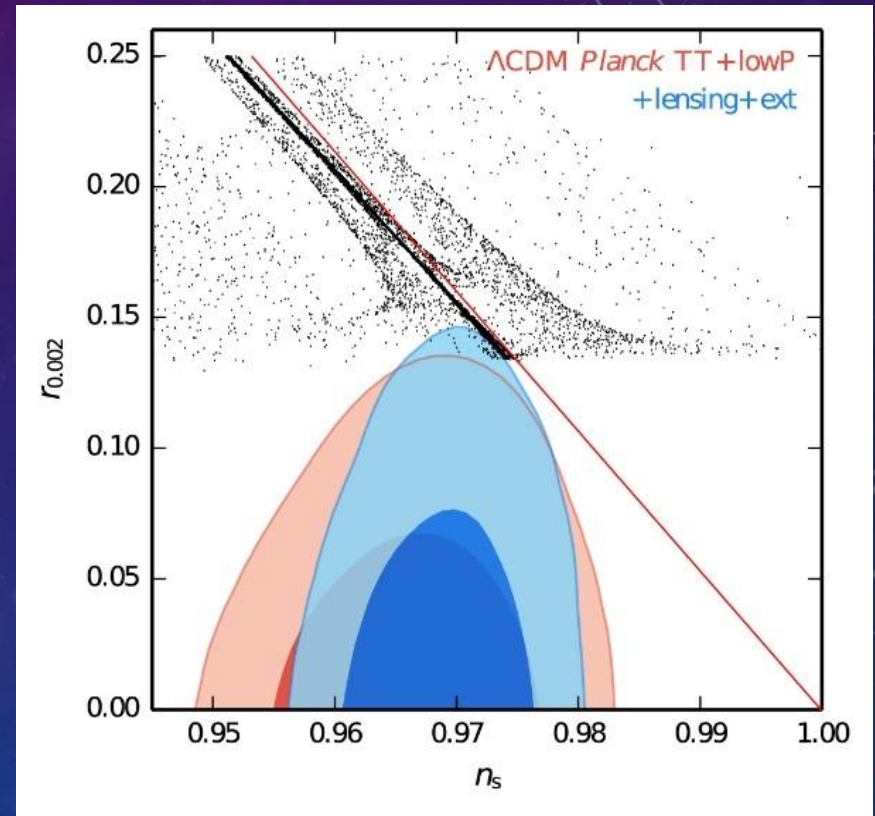
- Always constant $C \simeq -0,72$, however constant $\alpha = \frac{1}{6}$ for tachyon inflation in standard cosmology, and $\alpha = \frac{1}{12}$ for Randall-Sundrum cosmology

NUMERICAL RESULTS



OBSERVATIONAL PARAMETERS (n_s, r), $U(x) = \frac{1}{x^4}$

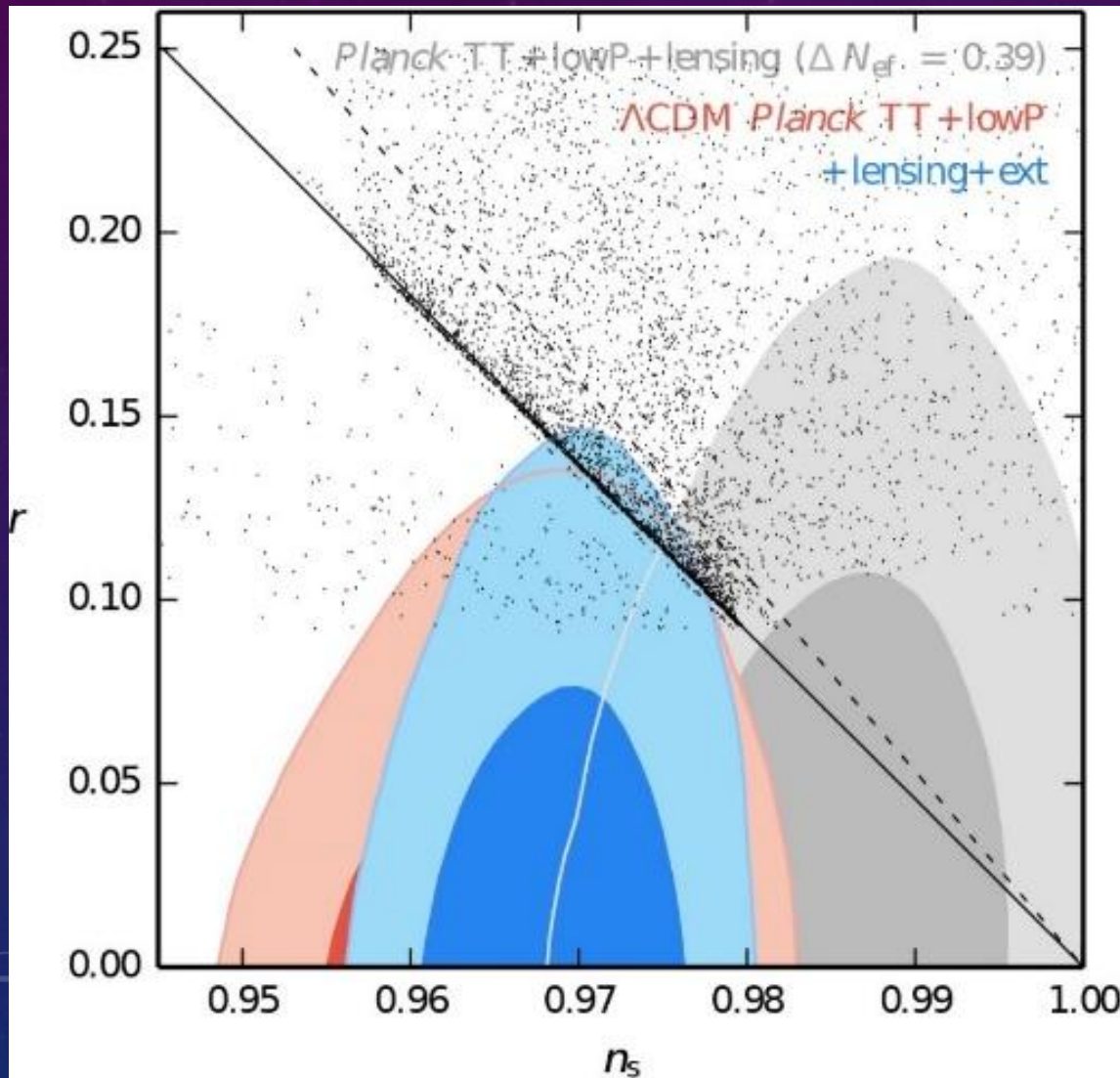
- Diagram with observational constraints from Planck 2015.
- The dots represent the calculation in the tachyon model for various N, κ
- 35% of calculated results for pairs of free parameters is represented in the plot.
- **Red solid line** represents the slow-roll approximation of the standard tachyon model with inverse quartic potential. $r = \frac{16}{3}(1 - n_s)$.



$$45 \leq N \leq 120$$

$$1 \leq \kappa \leq 25$$

OBSERVATIONAL PARAMETERS (n_s, r), RSII MODEL



- Free parameters from the interval:

$$60 \leq N \leq 120$$

$$1 \leq k \leq 12$$

$$0 \leq f_0 \leq 0,5$$

- Approximate relation:

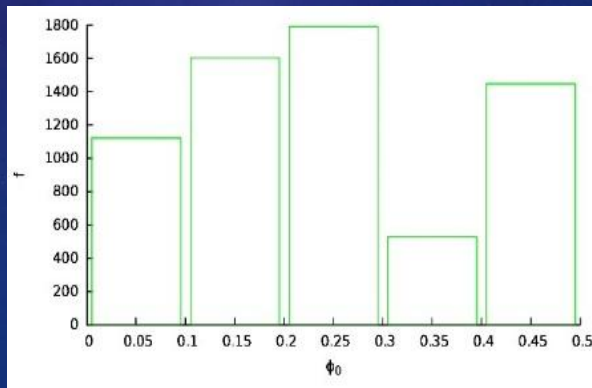
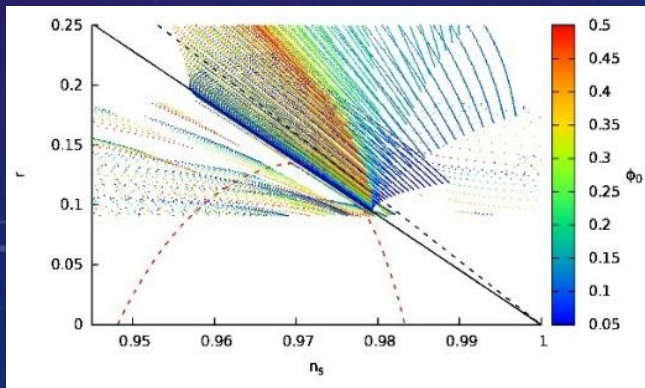
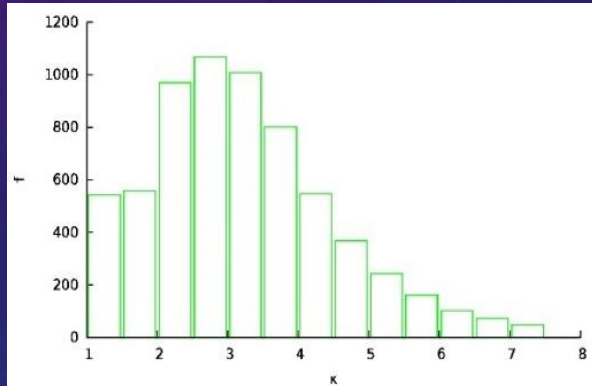
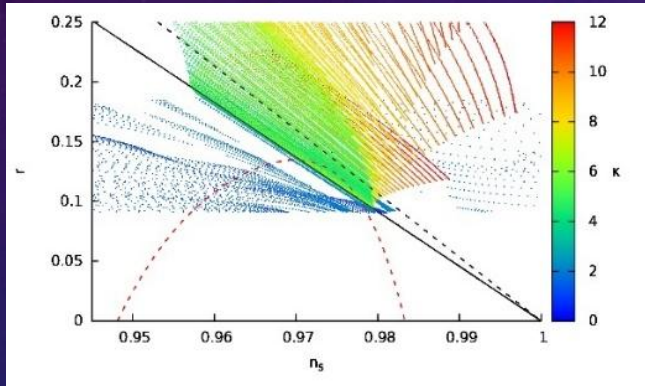
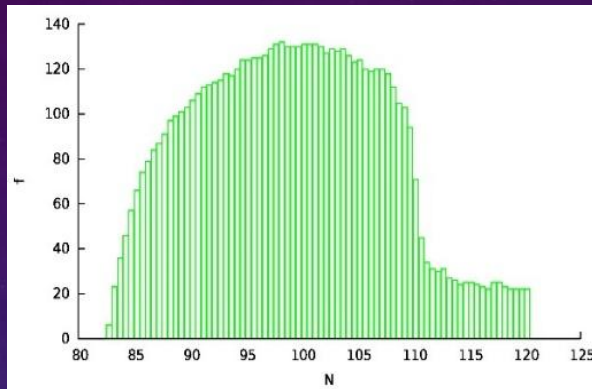
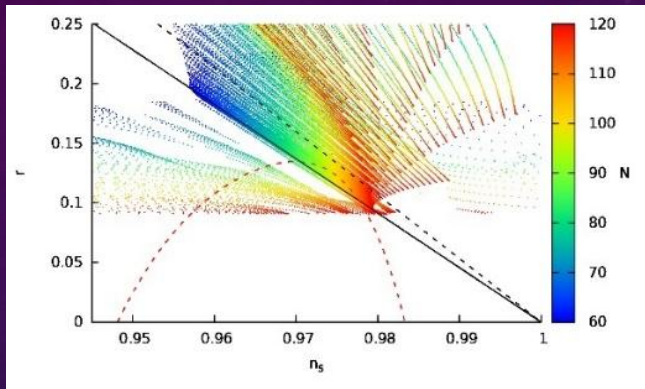
- RS model

$$r = \frac{32}{7}(1 - n_s) \quad \text{———}$$

- Tachyon model (FRW)

$$r = \frac{16}{3}(1 - n_s) \quad \text{--- --}$$

(n_s, r) AS A FUNCTION OF N, κ, ϕ_0



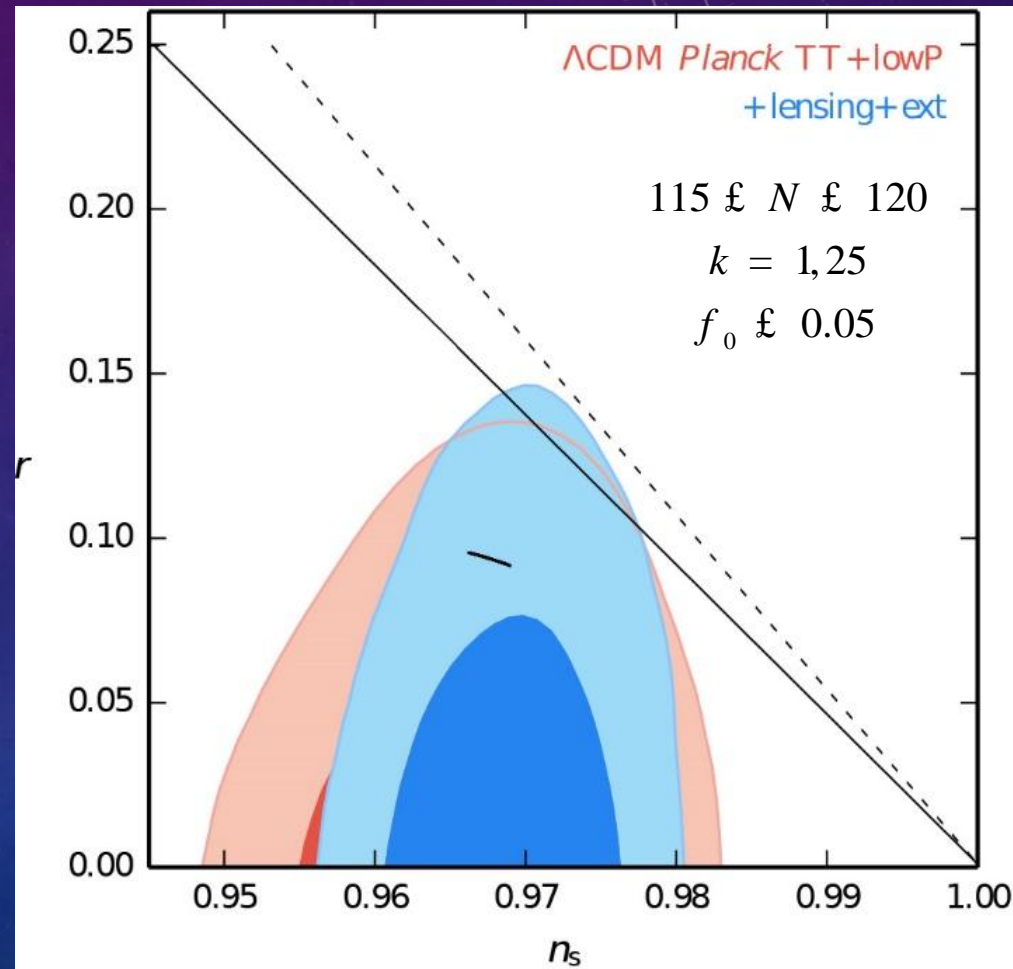
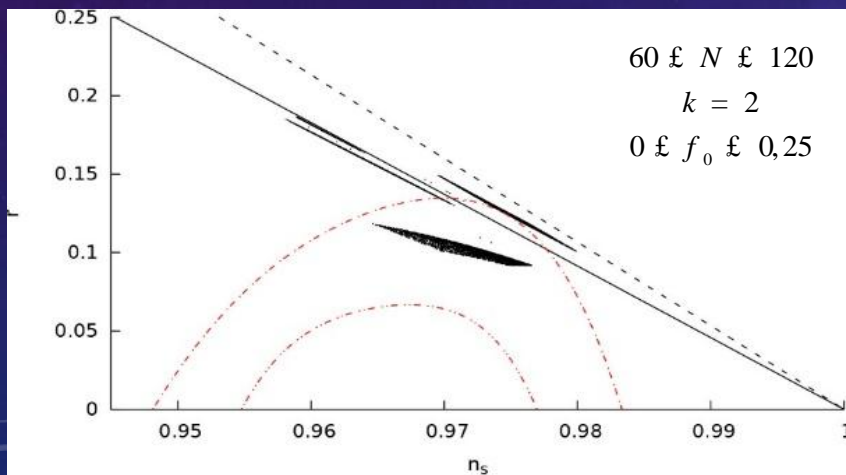
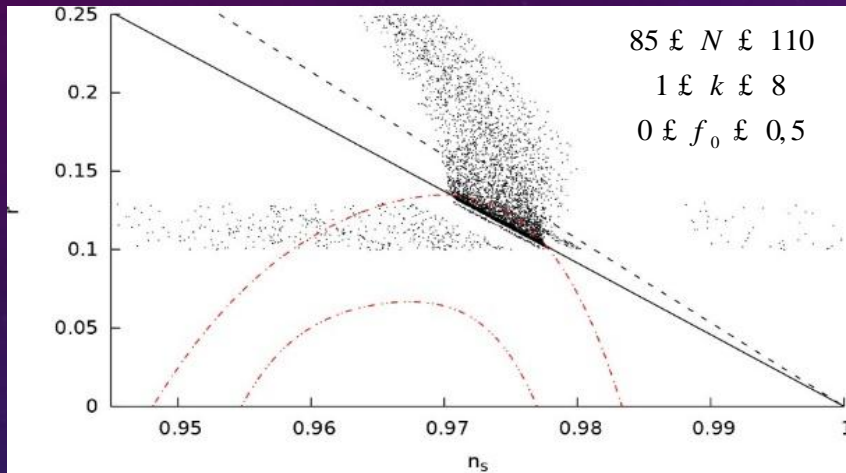
$60 \leq N \leq 120, \quad DN = 0,5$

$1 \leq k \leq 12, \quad Dk = 0,5$

$0 \leq f_0 \leq 0,5, \quad Df_0 = 0.05$

-
- 65% is plotted,
12% in 2σ range

THE BEST FITTING RESULTS (n_s, r)



TACHYON WITH AN INVERSE POWER-LAW POTENTIAL IN A BRANEWORLD COSMOLOGY

Here, we study a quite similar tachyon cosmological model based on the dynamics of a 3-brane in the bulk of the second Randall-Sundrum model extended to more general warp functions, i.e. with a selfinteracting scalar

- As a consequence, on the observer brane G is modified to be the scale dependent four-dimensional gravitational constant. A power law warp factor generates an inverse power-law potential $V \sim \phi$

TACHYON WITH AN INVERSE POWER-LAW POTENTIAL IN A BRANEWORLD COSMOLOGY

- Introducing a combined dimensionless coupling

$$\kappa^2 = \frac{8\pi G_5}{k} \sigma = \frac{8\pi G_N}{k^2} \sigma$$

- and dimensionless functions, in the same way as it was done for the previous models, we obtain the following set of equations

$$\dot{\phi} = \frac{\chi^4 \pi_\phi}{\sqrt{1 + \chi^8 \pi_\phi^2}} = \frac{\pi_\phi}{\rho}$$

$$\dot{\pi}_\phi = -3h\pi_\phi + \frac{4\chi_{,\phi}}{\chi^5 \sqrt{1 + \chi^8 \pi_\phi^2}}$$

- Where

$$h = \sqrt{\frac{\kappa^2}{3} \rho \left(\chi_{,\phi} + \frac{\kappa^2}{12} \rho \right)}, \quad \text{and} \quad \chi_{,\phi} = \frac{\partial \chi}{\partial \phi}$$

- We analyze in detail the tachyon with potential

$$\chi(\phi) = \phi^{n/4}$$

TACHYON WITH AN INVERSE POWER-LAW POTENTIAL IN A BRANEWORLD COSMOLOGY

- Following the similar procedure as in the previous RSII model, for a given N and κ initial condition for the tachyon field can be obtained from the slow-roll condition

$$N \approx \frac{2n}{(4n-1)\dot{\phi}_1(\phi_1)} - \frac{3n+1}{2(3n-1)}$$

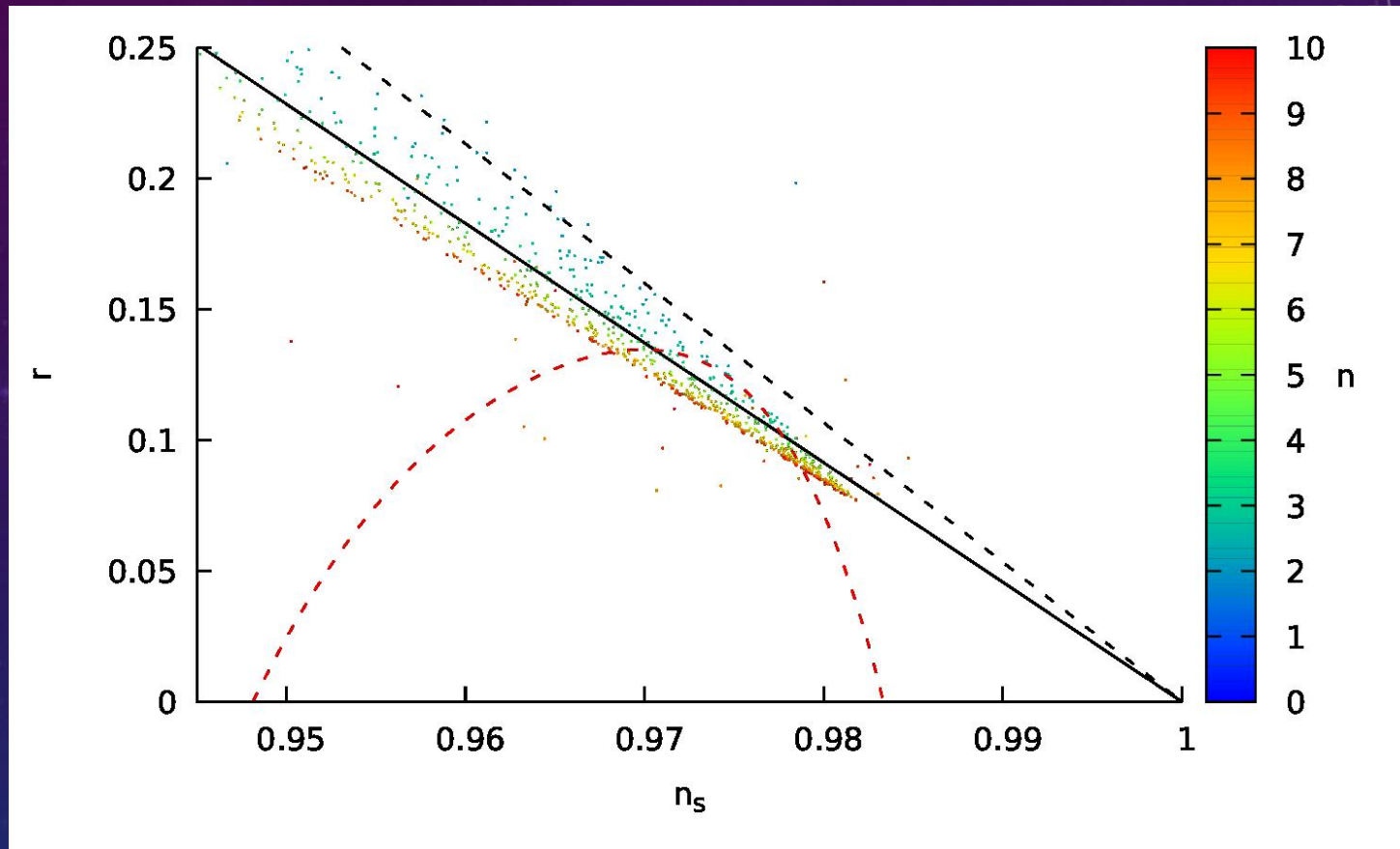
• Where

$$\dot{\phi}_1(\phi_1) \approx 192 \frac{\chi^6(\theta_i) \chi_{,\theta}^2(\theta_i)}{\kappa^4}$$

- Here, we find the critical value
``dust vs quasi de Sitter``.

$$n > \frac{1}{3}$$

NEW RESULTS



- 1000 randomly chosen values of free parameters (N, κ, n)

$$45 \leq N \leq 120$$

$$0.5 \leq \kappa \leq 10$$

$$0.5 \leq n \leq 10$$

ONGOING RESEARCH - RSII AND HOLOGRAPHIC COSMOLOGY

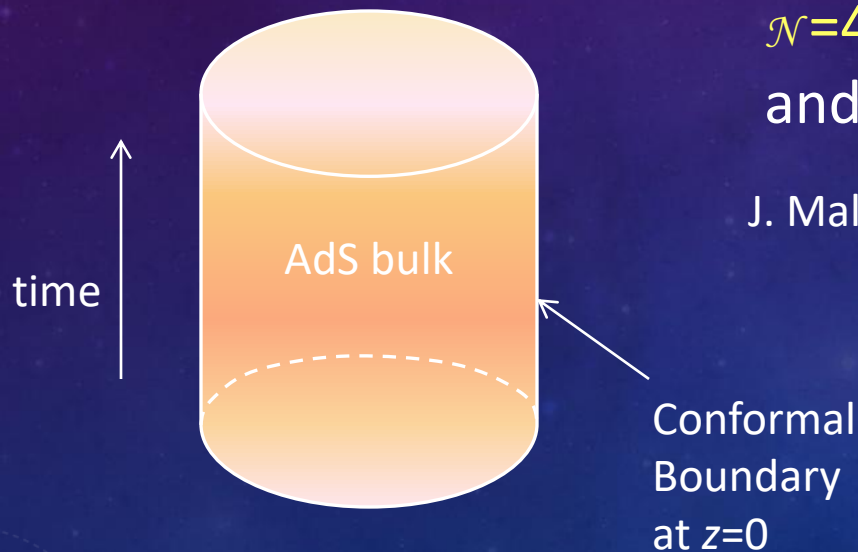
- Here we present unpolished results and ongoing work

Connection with AdS/CFT

AdS/CFT correspondence is a holographic duality between gravity in $d+1$ -dim space-time and quantum **CFT** on the d -dim boundary. Original formulation stems from string theory:

Equivalence of $3+1$ -dim
 $\mathcal{N}=4$ Supersymmetric YM Theory
and string theory in $\text{AdS}_5 \times S_5$

J. Maldacena, Adv. Theor. Math. Phys. 2 (1998)



Examples of CFT:
quantum electrodynamics,
 $\mathcal{N}=4$ Super YM gauge theory,
massless scalar field theory,
massless spin $\frac{1}{2}$ field theory

Holographic cosmology

We start from AdS-Schwarzschild static coordinates and make the coordinate transformation $t = t(\tau, z)$, $r = r(\tau, z)$. The line element will take a general form

$$ds_{(5)}^2 = \frac{\ell^2}{z^2} (g_{\mu\nu} dx^\mu dx^\nu - dz^2) = \frac{\ell^2}{z^2} \left[n^2(\tau, z) d\tau^2 - a^2(\tau, z) d\Omega_k^2 - dz^2 \right]$$

Imposing the boundary conditions at $z=0$:

$$n(\tau, 0) = 1, \quad a(\tau, 0) = a_h(\tau)$$

we obtain the induced metric at the boundary in the FRW form

$$ds_{(0)}^2 = g_{\mu\nu}^{(0)} dx_\mu dx_\nu = d\tau^2 - a_h^2(\tau) d\Omega_k^2$$

Solving Einstein's equations in the bulk one finds

$$a^2 = a_h^2 \left[\left(1 - \frac{\mathcal{H}_h^2 z^2}{4} \right)^2 + \frac{1}{4} \frac{\mu z^4}{a_h^4} \right], \quad n = \frac{\dot{a}}{\dot{a}_h},$$

where $\mathcal{H}_h^2 = H_h^2 + \frac{\kappa}{a_h^2}$ $H_h = \frac{\dot{a}_h}{a_h}$ Hubble rate at the boundary

P.S. Apostolopoulos, G. Siopsis and N. Tetradis, Phys. Rev. Lett. **102**, (2009)

Comparing the exact solution with the expansion

$$g_{\mu\nu} = g_{\mu\nu}^{(0)} + z^2 g_{\mu\nu}^{(2)} + z^4 g_{\mu\nu}^{(4)} + \dots$$

we can extract $g_{\mu\nu}^{(2)}$ and $g_{\mu\nu}^{(4)}$. Then, using the de Haro et al expression for \mathcal{T}^{CFT} we obtain

$$\langle T_{\mu\nu}^{\text{CFT}} \rangle = t_{\mu\nu} + \frac{1}{4} \langle T_{\alpha}^{\text{CFT}\alpha} \rangle g_{\mu\nu}^{(0)}$$

The second term is the conformal anomaly

$$\langle T_{\alpha}^{\text{CFT}\alpha} \rangle = \frac{3\ell^3}{16\pi G_5} \frac{\ddot{a}_h}{a_h} \mathcal{H}_h^2$$

The first term is a traceless tensor with non-zero components

$$t_{00} = -3t_i^i = \frac{3\ell^3}{64\pi G_5} \left(\mathcal{H}_h^4 + \frac{4\mu}{a_h^4} - \frac{\ddot{a}_h}{a_h} \mathcal{H}_h^2 \right)$$

Hence, apart from the conformal anomaly, the CFT dual to the time dependent asymptotically AdS_5 bulk metric is a conformal fluid with the equation of state $p_{\text{CFT}} = \rho_{\text{CFT}}/3$ where

$$\rho_{\text{CFT}} = t_{00} \quad p_{\text{CFT}} = -t_i^i$$

from Einstein's equations on the boundary we obtain the holographic Friedmann equation

$$\mathcal{H}_h^2 = \frac{8\pi G_N}{3} \rho_h + \frac{\ell^2}{4} \left(\mathcal{H}_h^4 + \frac{4\mu\ell}{a_h^4} \right)$$

quadratic deviation

dark radiation

Kiritsis, JCAP **0510** (2005) ; Apostolopoulos et al, Phys. Rev. Lett. **102**, (2009)

The second Friedmann equation can be derived from energy-momentum conservation

$$\frac{\ddot{a}_h}{a_h} \left(1 - \frac{\ell^2}{2} \mathcal{H}_h^4 \right) + \mathcal{H}_h^2 = \frac{4\pi G_N}{3} (\rho_h - 3p_h)$$

quadratic deviation

where $\rho_h = T_{00}^{\text{matt}}$, $p_h = -T^{\text{matt}i}_i$

Holographic map

The time dependent bulk spacetime with metric

$$ds_{(5)}^2 = \frac{\ell^2}{z^2} \left[n^2(\tau, z) d\tau^2 - a^2(\tau, z) d\Omega_k^2 - dz^2 \right]$$

may be regarded as a z -foliation of the bulk with FRW cosmology on each z -slice. In particular:

at $z=z_{\text{br}}$: RSII cosmology, at $z=0$: holographic cosmology.

A map between z -cosmology and $z=0$ -cosmology can be constructed using

$$a^2 = a_h^2 \left[\left(1 - \frac{\mathcal{H}_h^2 z^2}{4} \right)^2 + \frac{1}{4} \frac{\mu z^4}{a_h^4} \right], \quad n = \frac{\dot{a}}{\dot{a}_h},$$

and the inverse relation

$$a_h^2 = \frac{a}{2} \left(1 + \frac{\mathcal{H}^2 z^2}{2} + E \sqrt{1 + \mathcal{H}^2 z^2 - \frac{\mu z^4}{a^4}} \right) \quad E = \begin{cases} \pm 1 & \text{one-sided} \\ -1 & \text{two-sided} \end{cases}$$

Holographic map

holographic
cosmology

$$z = 0$$

$$ds_h^2 = d\tau^2 - a_h^2 d\Omega_k^2$$

$$\tau \rightarrow \tilde{\tau}$$

$$ds_h^2 = \frac{1}{n^2} d\tilde{\tau}^2 - a_h^2 d\Omega_k^2$$

$$z$$



$$z = z_{\text{br}}$$

$$ds^2 = n^2 d\tau^2 - a^2 d\Omega_k^2$$

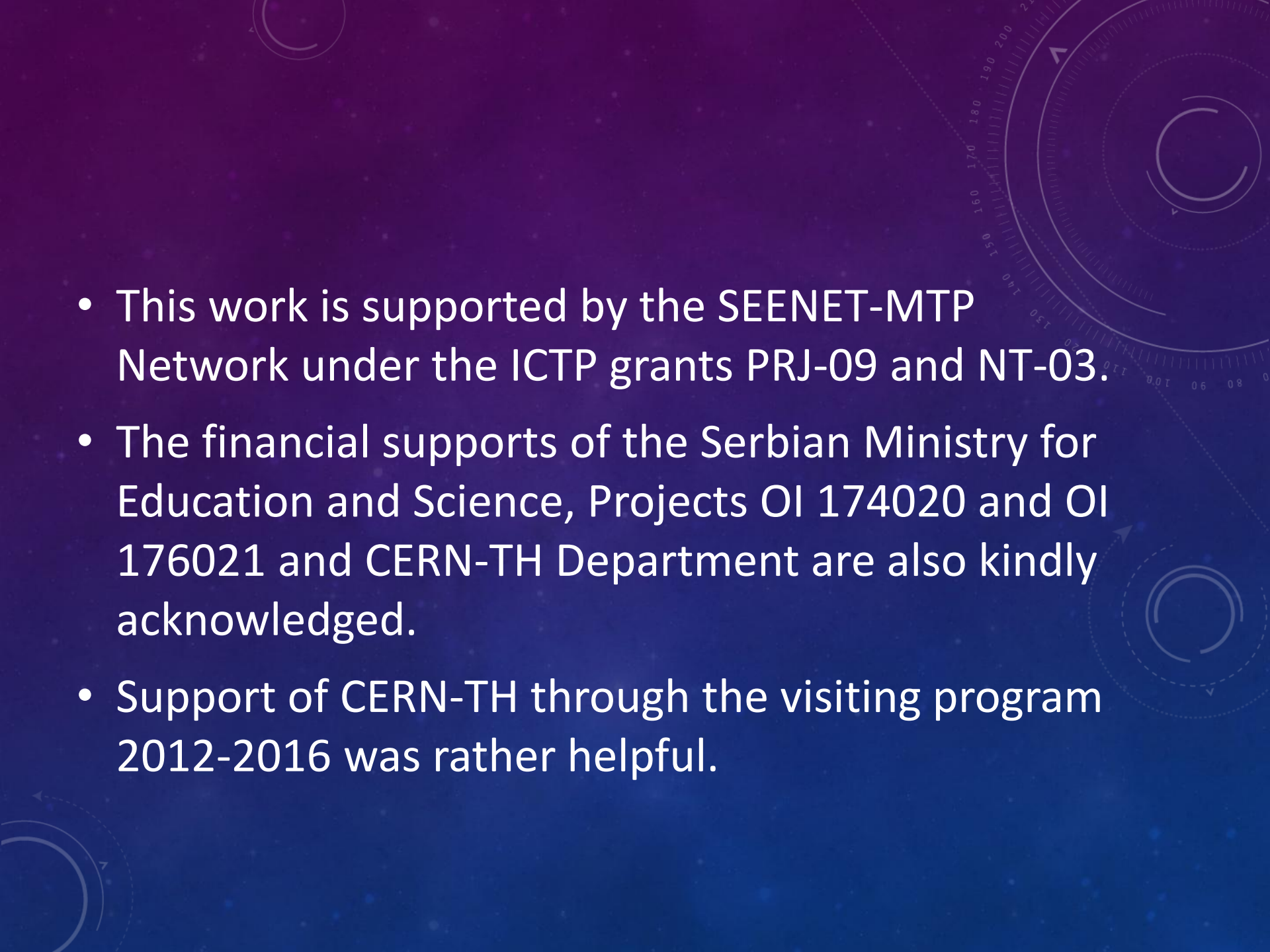
$$\tau \rightarrow \tilde{\tau}$$

$$ds^2 = d\tilde{\tau}^2 - a^2 d\Omega_k^2$$

RSII
cosmology

CONCLUSION

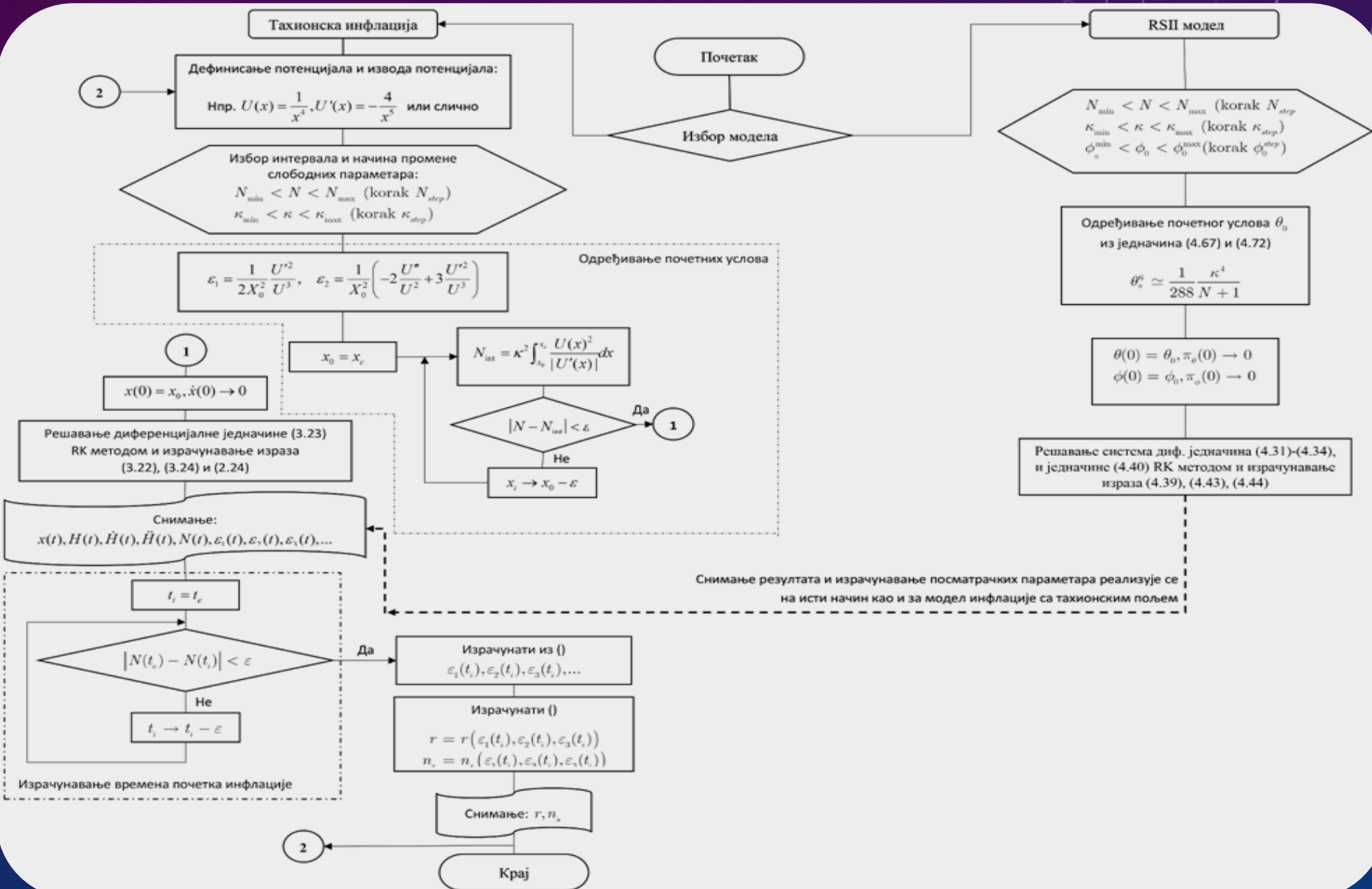
- We have investigated a model of inflation based on the dynamics of a D3-brane in the AdS_5 bulk of the RSII model. The bulk metric is extended to include the backreaction of the radion excitations.
- The agreement with observations is not ideal, the present model is disfavored but not excluded. However, the model is based on the brane dynamics which results in a definite potential with one free parameter only.
- The simplest tachyon model that stems from the dynamics of a D3-brane in an AdS_5 bulk yielding basically an inverse quartic potential.
- The same mechanism lead to a more general tachyon potential if the AdS_5 background metric is deformed by the presence of matter in the bulk, e.g. in the form of a minimally coupled scalar field with an arbitrary self-interaction potential. Critical values for the inverse power potential are found.

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- The background is a dark blue gradient with faint, stylized circular patterns and a scale-like graphic on the right side. The scale has numbers from 0 to 200 and arrows indicating a clockwise direction. There are also some smaller circular elements with arrows in the bottom left corner.
- This work is supported by the SEENET-MTP Network under the ICTP grants PRJ-09 and NT-03.
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NUMERICAL (PSEUDO)ALGORITAM



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- THANK YOU!!!

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